

A Level Statistics

AQA Past Exam Questions

Solutions

TOPIC: Least Squares Regression

In the new specification you will not be asked to calculate the values of a and b in any way other than on the calculator. You will not be asked to plot or draw a scatter graph or the LSR on a scatter graph so these questions from past papers have been omitted.

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions **on paper**
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Unless otherwise stated, statistical tests should be carried out at the 5% significance level.
- When a calculator is used, the answer should be given to three significant figures unless otherwise stated.

Information

- **You may use the** booklet 'Statistical Formulae and Tables'
- There are **12** questions in this question paper. The total mark for this paper is **123**
- The marks for **each** question are shown in brackets – use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.
- Check your answers if you have time at the end.

Q	Solution	Marks	Total	Comments
5	See supplementary sheet for alternative solutions and additional guidelines to parts (b), (d) and (e)			
(a)	Calorific value depends upon moisture content Moisture (content) is set/are fixed values	B1	1	Must be in context; not "it", etc Use of x and $y \Rightarrow$ B0
(b)	b (gradient) = -0.076 b (gradient) = -0.07 to -0.08 a (intercept) = 5.35 to 5.36 a (intercept) = 5.1 to 5.6 Thus $y = (5.35$ to $5.36) - 0.076x$	B2 (B1) B2 (B1) BF1		AWRT; including $-ve$ sign (-0.07582) AWFW; including $-ve$ sign <i>Treat rounding of correct answers as ISW</i> AWFW (5.35385) AWFW F on a and b even if rounded
(c)	a : calorific value of wood with zero/no moisture or dry maximum calorific value b : each 1(%) rise in moisture content reduces calorific value by 0.076 MWh/tonne As x increases y decreases	B1 B2 (B1)	3	OE; $a \leq 0 \Rightarrow$ B0 In context and with values; F on b $b \geq 0 \Rightarrow$ B0 Negative relationship/correlation
(d)	$y_{27} = 3.28$ to 3.32 $= 2.5$ to 3.5	B2 (B1)	2	AWFW (3.30659) AWFW; even if by interpolation from original data giving likely values of 3 or 3.04
(e)	$r(35, 2.5) = -0.21$ to -0.19 $= 0.1$ to 0.3	B2 (B1)	2	AWFW; including $-ve$ sign (-0.20000) AWFW; ignore sign
(f)	Good/reasonable/accurate/correct/etc Accept more positive qualifying adjectives	B1	1	OE; ignore reasoning Very good (B1) Not good (B0)
(g)(i)	Extrapolation/outside (observed) range (of x)	B1	1	OE
(ii)	$y_{80} = -0.5$ to -1 Negative value for calorific value is impossible or More energy needed than is generated	B1 Bdep1	2	AWFW (-0.71209) OE; dependent on B1 Must be in context; negative value impossible \Rightarrow Bdep0

Q	Solution	Marks	Total	Comments
1 (a)	$a = \underline{30}$	B1	1	CAO
(b)(i)	$b \text{ (gradient)} = \underline{-0.64}$ $b \text{ (gradient)} = \underline{-0.6 \text{ to } -0.7}$ $a \text{ (intercept)} = \underline{31}$ $a \text{ (intercept)} = \underline{30 \text{ to } 32}$	B2 (B1)		CAO AWFW <i>Treat rounding of correct answers as ISW</i> <i>Written form of equation is not required</i> CAO AWFW
	Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ $(\sum y^2)$ or Attempt at S_{xx} & S_{xy} (S_{yy}) Attempt at correct formula for b (gradient) $b \text{ (gradient)} = \underline{-0.64}$ $a \text{ (intercept)} = \underline{31}$	(M1) (m1) (A1 A1)	4	225 7125 135 & 2415 (2643) (all 4 attempted) 1500 & -960 (618) (both attempted) CAO both
(ii)	Candle length reduces by 0.64 (cm) per hour Candle burns 0.64 (cm) each/per hour Candle reduces by -0.64 (cm) each/per hour (Length, y , cm) decreases with (time, x , hours) or As (time, x , hours) increases then (length, y , cm) decreases	B1 BF1 (BF2) (BF1)		OE; must be in context OE; must be in context OE; must be in context OE; must be in context (double -ve) F on $-0.6 \leq b \leq -0.7$ from (i) OE; context not required B0 for reference only to correlation
(iii)	When $x = 50$, $y = (31 \text{ or } 30) - 0.64 \times 50$ = <u>-1 or -2</u> or When $y = 0$, $x = 31 \div 0.64 = \underline{48 \text{ to } 48.5}$ or $30 \div 0.64 = \underline{46.8 \text{ to } 47}$	B1	2	CAO; accept correct comparison of 32 with either 30 or 31 AWFW AWFW
	Claim not justified or -1 is impossible or value < 50 Claim cannot be answered due to uneven burning or unlikely to burn completely	Bdep1 (B1)	2	OE; dependent on previous B1 Extrapolation required

3(a)	b (gradient) = 7.05 b (gradient) = 7(0.0) to 7.1(0)	B2 (B1)	4	AWRT AWFW Treat rounding of correct stated answers as ISW	(7.05134)
	a (intercept) = 2500 to 2502 a (intercept) = 2490 to 2510	B2 (B1)		AWFW AWFW	(2501.091)
	or Attempt at $\sum x \sum x^2 \sum y \ \& \ \sum xy \ (\sum y^2)$	(M1)		1351 268047 27034 & 5269065 (105653202) (all 4 attempted)	
	or Attempt at S_{xx} & S_{xy} (S_{yy})	(m1)		7304 & 51503 (1247894) (both attempted)	
	Attempt at correct formula for b (gradient) b (gradient) = 7.05 a (intercept) = 2500 to 2502	(A1) (A1)		AWRT AWFW	
	Accept a & b interchanged only if identified correctly by a clearly shown equation (stated answers are not sufficient) in (b)			If a and b are not identified anywhere in solution, then: 7.05 \Rightarrow B1 2500 to 2502 \Rightarrow B1	
(b)	$y_{200} = a + b \times 200$ $= 3890$ to 3930	M1		Used May be implied by correct answer	
		A1	2	AWFW	(3911.36)
(c)	Large residuals / residual range suggest estimate may be unreliable or Largest residuals only small in relation to y -values (10%) so estimate may be reliable (unreliable)	B1 B1dep	2		
	Special Case: If B0 B0dep then: Involves interpolation Does not involve extrapolation Within observed range	B1 B1dep		(unreliable) requires (10% or equivalent)	
		(B1)		Any one; or equivalent	

5(a)	Time taken is dependent upon leaving time	B1	1	Or equivalent
(b)	b (gradient) = 1.28 (or 141/110) b (gradient) = 1.25 to 1.35 a (intercept) = 29.95 to 30 (or 659/22) a (intercept) = 29 to 31 Thus $y = 30 + 1.28x$ or Attempt at $\sum x$ $\sum x^2$ $\sum y$ and $\sum xy$ ($\sum y^2$) or Attempt at S_{xx} and S_{xy} (S_{yy}) Attempt at correct formula for b gradient b (gradient) = 1.28 (or 141/110) a (intercept) = 29.95 to 30 (or 659/22) Thus $y = 30 + 1.28x$ Accept a and b interchanged only if identified correctly by a clearly shown equation	B2 (B1) B2 (B1) B1F (M1)	5	AWRT; (CAO or equivalent) (1.28182) AWFW Treat rounding of correct answers as ISW AWFW; (CAO or equivalent) (29.95455) AWFW F on a and b 275 9625 682 and 20575 (47494) (All four attempted) 2750 and 3525 (5210) (Both attempted) AWRT; (CAO or equivalent) AWFW; (CAO or equivalent) F on a and b If a and b are not identified anywhere in the question, then: 1.25 to 1.35 \Rightarrow B1 29 to 30 \Rightarrow B1
(c)	$7.45 \text{ am} \Rightarrow x = 15$ $\Rightarrow y_{15} = 30 + 1.28 \times 15$ $= 47 \text{ to } 52$ Time before 9.00 am = $9.00 - (7.45 + c's y_{15})$ $= 23 \text{ to } 28$ SC Answer of 17 CAO (use of $c's y_{15} = 58$) gains 2 marks	B1 M1 A1 M1 A1	5	CAO; stated, used or implied Use of $10 < x < 20$ AWFW (49.2) May be implied AWFW (25.8) NB: An answer of 8.32 to 8.37 gains B1 M1 A1 M0 A0
(d)(i)	$y_{85} = 30 + 1.28 \times 85 = 135 \text{ to } 146$	B1	1	AWFW (138.9)
(ii)	Extrapolation/ outside/ above range of x -values Implies leaves home at 8.55 so different traffic conditions	B1 B1	2	Or equivalent Or equivalent; 8.55 may be implied by 5 minutes

1(a)	b (gradient) = -1.01 to -1(00) (b (gradient) = -1.05 to -0.95)	B2 (B1)		AWFW	(-1.00337)
	a (intercept) = 53(.0) to 53.2 (a (intercept) = 52(.0) to 54(.0))	B2 (B1)	4	AWFW	(53.06736)
	OR				
	Attempt at $\sum x$, $\sum x^2$, $\sum y$ and $\sum xy$			180, 3986, 297 and 5552.7	
	or	(M1)			
	Attempt at S_{xx} and S_{xy}			386 and -387.3	
	Attempt at correct formula for b (gradient)	(m1)			
	b (gradient) = -1.01 to -1(00)	(A1)		AWFW	
	a (intercept) = 53(.0) to 53.2	(A1)		AWFW	
	Accept a and b interchanged only if then identified correctly in part (b), but B2 in (b) does not necessarily imply 4 marks in (a)				
(b)	When $x = 21$,				
	$y = 31.7$ to 32.2 ($y = 29.9$ to 34.1)	B2 (B1)	2	AWFW AWFW	(32.0)
	Evidence of use of 21 in c's equation	(M1)			
	<i>Special Cases (if seen):</i>				
	$y = \frac{33.0 + 30.7}{2} = 31.8$ to 31.9	(B1)		AWFW; or equivalent	
	$y = 31.85$ without working	(B1)			

5(a)	Time taken depends upon temperature	B1	1	OE; not x set values
(b)	b (gradient) = -0.0873 to -0.087 b (gradient) = -0.09 to -0.08	B2 (B1)		AWFW AWFW; $-8.73^{-02} \Rightarrow B0$ $(-0.087\dot{2}\dot{7})$
	a (intercept) = 5.94 to 5.96 a (intercept) = 5.6 to 6.1	B2 (B1)		AWFW AWFW $(5.95\dot{0}\dot{9})$
	Attempt at $\sum x$, $\sum x^2$, $\sum y$ and $\sum xy$ or Attempt at S_{xx} and S_{xy} Attempt at correct formula for b $b = -0.0873$ to -0.087 $a = 5.94$ to 5.96	(M1) (m1) (A1) (A1)	4	396, 16016, 30.9 and 958.8 1760 and -153.6 AWFW AWFW
	Accept a and b interchanged only if then identified correctly later in question			
(c)(i)	Each 1°C rise in temperature results in an (average) decrease of 0.087 m (5 s) in time taken for pellets to dissolve	B1 B1	2	Quantified rise in x (results in) Decrease in y OE
(ii)	a is y -value at $x = 0$ at which water is solid/ice/frozen so pellets cannot dissolve	B1 B1	2	Indication that it is y at $x = 0$ Mention of solid or ice or frozen
(d)(i)	When $x = 30$ $y = 3.3$ to 3.4 $y = 2.9$ to 3.7	B2 (B1)		AWFW AWFW $(3.33\dot{2}\dot{7})$
	If B0, use of their equation with $x = 30$	(M1)	2	
(ii)	When $x = 75$ $y < 0$ or negative which is impossible	B1 \uparrow Dep \uparrow B1	2	OE OE; not extrapolation

4(a)	b (gradient) = -0.5485 to -0.5475	B2		AWFW	(-0.54814)
	b (gradient) = -0.55 to -0.54	(B1)		AWFW	
	Omission of $-ve$ sign	(B0)			
	a (intercept) = 49.7 to 49.9	B2		AWFW	(49.7982)
	a (intercept) = 49 to 50	(B1)		AWFW	
	or				
	Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ ($\sum y^2$)	(M1)		305 14975 281 & 6980 (10173) (all 4 attempted)	
	or			4638.89 & -2542.78 (both attempted)	
	Attempt at S_{xx} & S_{xy}				
	Attempt at correct formula for b (gradient)	(m1)			
	b (gradient) = -0.5485 to -0.5475	(A1)		AWFW	
	a (intercept) = 49.7 to 49.9	(A1)	4	AWFW	
	Accept a & b interchanged only if identified correctly by a clearly shown equation (stated answers are not sufficient) in (b) or (c)			If a and b not identified anywhere in question, then: -0.5485 to $-0.5475 \Rightarrow B1$ 49.7 to $49.9 \Rightarrow B1$	
(b)	C's value of intercept from (a) providing > 47			Accept value rounded to nearest integer	(50)
	or		1		
	Value 50 stated even if (a) incorrect or not attempted	B1F			
(c)	13 weeks $\Rightarrow 91$ days	B1		Stated or used	
				Accept a descriptive answer that includes 91 and a value in range	
	$y = -1.1$ to $+ 1.1$	B1		AWFW	(-0.08254)
	or				
	$y = 0 \Rightarrow x = 89$ to 93	(B1)		AWFW	(90.84942)
				Accept a descriptive answer that includes a value in range and 13	
	$\Rightarrow 13$ weeks (approximately)	(B1)		Stated	
Note:					
	B1 B1 or (B1) (B1) are available even if (a) not attempted				
	or				
	Thus claim appears justified	B1 dep		Or equivalent; ignore reasoning unless contradictory	
	or			Dependent upon 2 nd B1 in (c) or 2 nd (B1) in (c)	
	Thus tablet likely to have dissolved				
	or				
	Extrapolation required so cannot comment	(B1)		Not dependent	
Note:					
	If (B1) for extrapolation maximum mark is 2; other mark available is for 91		3		

3	<p>(a) b (gradient) = 191 b (gradient) = 190 to 192</p> <p>a (intercept) = 115 a (intercept) = 93 to 137</p> <p>OR</p> <p>Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ ($\sum y^2$)</p> <p>or</p> <p>Attempt at S_{xx} & S_{xy} (S_{yy})</p> <p>Attempt at correct formula for b (gradient) b (gradient) = 191 a (intercept) = 115</p> <p>Accept a & b interchanged only if identified and used correctly in (ii)</p>	<p>B2 (B1)</p> <p>B2 (B1)</p> <p>(M1)</p>	4	<p>CAO AWFW <i>Treat rounding of correct answers as ISW</i></p> <p>CAO AWFW</p> <p>154 3452 30219 & 677042 (133170091) (all 4 attempted)</p> <p>12224 & 64 (2714668) (both attempted)</p> <p>CAO CAO</p> <p>If a and b are not identified anywhere in question, then: 190 to $192 \Rightarrow B1$ 93 to $137 \Rightarrow B1$</p>
(ii)	<p>$y_{24} = 115 + 191 \times 24$ $= \text{£4699 or £4700}$ $= \text{£4650 to £4750}$</p> <p>SC: $(4290 + 5057)/2 = 4673$ to $4674 \Rightarrow B1$</p> <p>If B0 but clear evidence of correct use of c's equation with $x = 24$</p>	<p>B2 (B1)</p> <p>(M1)</p>	2	<p>Either; ignore units AWFW</p> <p>(£4699)</p>
(iii)	<p>(Maximum) temperature (in February) is likely to be/will be lower/different</p> <p>Must imply a temperature comparison with July</p>	<p>B1</p>	1	<p>Or equivalent; must be clear indication that (max) temperature is less than/different</p> <p>Extrapolation/not July/not summer/winter/etc $\Rightarrow B0$</p>
(iv)	<p>Rainfall amount/wind strength/sunshine hours/daylight hours/opening times/day of week/visitor numbers/public holidays/school holidays/local attractions/etc</p> <p>Allow if at least 1 variable correctly identified</p>	<p>B1</p>	1	<p>Or equivalent</p> <p>Accept any sensible reason; do not penalise for dubious 'variable name' so, for example, accept 'rainfall'</p> <p>Minimum/average temp/etc $\Rightarrow B0$</p> <p>Quality or price of food/staff/etc $\Rightarrow B0$</p>

3	No MR or MC in this question	B2 (B1)		AWRT AWFW AWFW AWFW	(0.85055) (94.69602)
	b (gradient/slope) = <u>0.85</u> b (gradient/slope) = <u>0.8 to 0.9</u>				
Notes	a (intercept) = <u>94.6 to 94.8</u> a (intercept) = <u>93 to 97</u>	B2 (B1)			
	Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$	(M1)		254 6924 1163 & 29942 (all 4 attempted) $(\sum y^2 = 135693)$	
	or			472.4 & 401.8 (both attempted) $(S_{yy} = 436.1)$	
	Attempt at correct formula for b	(m1)			
	$b = 0.85$ (AWRT) $a = 94.6$ to <u>94.8</u> (AWFW)	(A1 A1)	4	$(\bar{x} = 25.4$ & $\bar{y} = 116.3)$	
	1 Treat rounding of correct answers as ISW			2 Written form of equation is not required	
	3 Award 4 marks for $y = (94.6$ to <u>94.8</u>) + 0.85 or for $(94.6$ to <u>94.8</u>) + 0.85x				
	4 Values of a and b interchanged and equation $y = ax + b$ stated in (b) \Rightarrow max of 4 marks				
	5 Values of a and b interchanged and equation $y = a + bx$ stated in (b) \Rightarrow 0 marks				
(b)	$y_{30} = 120$ to <u>120.5</u> $y_{30} = 117$ to <u>123</u>	B2 (B1)	2	AWFW AWFW	(120.21253)
	1 If, and only if, B0, then award M1 for seen use of $y = a + bx \times 30$				
(c)(i)	Extrapolation BMI is outside/above range 45 is outside/above range of BMI or x	B1		OE; accept references to sample/data but not to population	
	Extrapolation Age is outside/above range 50 is outside/above range of age	B1	2	OE; accept references to sample/data but not to population	
Notes	1 Extrapolation only stated in each of (i) & (ii) \Rightarrow B1 B0			2 Two debateable answers \Rightarrow B1 max	
(d)	$r_{20} = 117 - (a + b \times 20) = 5.3$ $= 5$ to <u>6</u>	B2 (B1)	2	AWRT; do not ignore sign (5.29297) AWFW; ignore sign	
	1 If, and only if, B0, then award M1 for seen use of $\pm [117 - (a + b \times 20)]$				
(e)	As 2.71/(mean) value is small (in comparison to y -values), estimate is likely to be (quite/fairly/very/extremely) accurate	B1	1	OE; justification & conclusion	

5(a) (i)	b (gradient/slope) = <u>0.372 to 0.373</u> b (gradient/slope) = <u>0.3 to 0.4</u>	B2 (B1)		AWFW AWFW	(0.37235)
	a (intercept) = <u>6.94 to 6.95</u> a (intercept) = <u>6 to 9</u>	B2 (B1)		AWFW AWFW	(6.94648)
	Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ or Attempt at S_{xx} & S_{xy} Attempt at substitution into correct corresponding formula for b $b = \underline{0.372 \text{ to } 0.373}$ $a = \underline{6.94 \text{ to } 6.95}$	(M1) (m1) (A1 A1)		324 8922.70 204 & 5573.05 (all 4 attempted) $(\sum y^2 = 3493.64)$ 174.70 & 65.05 (both attempted) $(S_{yy} = 25.64)$ AWFW 4	$(\bar{x} = 27 \text{ & } \bar{y} = 17)$
Notes	1 Written form of equation is not required 2 Award 4 marks for $y = (6.94 \text{ to } 6.95) + (0.372 \text{ to } 0.373)x$ or for $(6.94 \text{ to } 6.95) + (0.372 \text{ to } 0.373)x$ 3 Values of a and b interchanged and equation $y = ax + b$ stated or used in (b) or (c) \Rightarrow max of 4 marks 4 Values of a and b interchanged and equation $y = a + bx$ stated or used in (b) & (c) \Rightarrow 0 marks 5 Values are not identified, then \Rightarrow B0 B0 6 Some/all of marks can be scored in (a)(ii), (a)(iii), (b) & (c)(i), even if some/all of marks are lost in (a)(i), but marks lost in (a)(i) cannot be recouped by subsequent working in (a)(ii), (a)(iii), (b) or (c)(i) but see Note 3				
(ii)	Each/every/one degree ($^{\circ}\text{C}$) rise in ground temperature results in or increase per degree ($^{\circ}\text{C}$) is (on average) b vibrations per second	B1 BF1	2	F on b providing $0.3 \leq b \leq 0.4$	
Notes	1 To score any marks, an explanation must indicate change in x affecting change in y , not change in y affecting change in x 2 Accept, for example, 10 $^{\circ}\text{C}$ and 10 b vibrations 3 Reference only to correlation \Rightarrow B0 BF0				
SC	1 As x /temperature increases (by c) then y /vibrations increases by b (OE; value of b ($0.3 \leq b \leq 0.4$) must be stated but context and/or units are not required) \Rightarrow B1				
(iii)	Given: When temperature/ $x < 15^{\circ}\text{C}$ or $= 0^{\circ}\text{C}$ value of $y = \underline{0}$ Equation: When temperature/ $x = 0^{\circ}\text{C}$ vibrations/value of $y = \underline{6 \text{ to } 9}$	B1 BF1	2	Must be stated clearly AWFW F on a providing $6 \leq a \leq 9$	
Notes	1 B1 is for a clear statement of information given in the question in terms of temperature/ x and y 2 BF1 is for a clear statement of the value of vibrations/ y shown by the equation when temperature/ $x = 0$				
5	Continued		8		
(b)	$y(23) = \underline{15.4 \text{ to } 15.6}$	B1	1	AWFW	(15.51059)
Note	1 Ignore any method shown				
(c) (i)	$\text{res}(28.6) = 17.0 - a - b \times 28.6$ $= \underline{-0.55 \text{ to } -0.65}$ $= \underline{0.5 \text{ to } 0.7}$	B2 (B1)	2	AWFW; do not ignore sign (-0.59576) AWFW; ignore sign	
Note	1 If, and only if, B0, then attempted use of $\pm(17.0 - a - b \times 28.6) \Rightarrow$ M1 providing $0.3 \leq b \leq 0.4$ and $6 \leq a \leq 9$				
(ii)	Value will be/is always: <u>0 or zero or nought or nothing or nil</u>	B1	1	CAO; accept nothing else, but ignore zeros after decimal point (eg 0.00) Ignore any explanation	

2 (a)	b (gradient/slope) = <u>-0.574 to -0.575</u> b (gradient/slope) = <u>-0.5 to -0.6</u>	B2 (B1)		AWFW AWFW	(-0.574515)
	a (intercept) = <u>50.9 to 51.0</u> a (intercept) = <u>46 to 53</u>	B2 (B1)		AWFW AWFW	(50.947359)
	<u>$y = (46 \text{ to } 53) - (0.5 \text{ to } 0.6)x$</u>	B1			
OR					
	Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ or Attempt at S_{xx} & S_{xy} Attempt at substitution into correct corresponding formula for b $b = \text{-0.574 to -0.575}$ $a = \text{50.9 to 51.0}$	(M1) (m1) (A1 A1)		570 32825.1 182 & 10181.48 (all 4 attempted) $(\sum y^2 = 3441.64)$ 335.1 & -192.52 (both attempted) $(S_{yy} = 129.24)$	$(\bar{x} = 57 \text{ & } \bar{y} = 18.2)$
	<u>$y = (46 \text{ to } 53) - (0.5 \text{ to } 0.6)x$</u>	B1			
Notes	1 Values of a and b interchanged or not identified but equation $y = ax + b$ stated \Rightarrow max of 5 marks 2 Values of a and b interchanged or not identified and equation $y = a + bx$ stated \Rightarrow 0 marks		5		
(b) (i)	$y_{(60.0)} = \text{16.3 to 16.6}$	B1	1	AWFW	(16.476455)
(ii)	Women/sample selected could be: or Under 45 or Over 65 Not between 45 and 65 or No previous browsing/IT experience No internet/IT access	B1 B1		OE; must reference age/years Accept "less experience" OE Accept "limited access"	
			2		

5	(a) x is the independent/controlled variable x are set values/percentages y is the response/dependent variable y are measured values/degrees y depends on x or x does not depend on y	B1		OE
			1	
(b) (i)	b (gradient/slope) = <u>-0.485</u> b (gradient/slope) = <u>-0.47 to -0.50</u> a (intercept) = <u>0.278 to 0.729</u>	B2 (B1)		CAO AWFW AWFW (0.50357)
	or $\sum x = 105$ $\sum x^2 = 2275$ $(\sum y^2 = 487.5)$ $\sum y = -47.4$ $\sum xy = -1050.5$ or $S_{xx} = 700$ $S_{xy} = -339.5$ $(S_{yy} = 166.53429)$ b (gradient/slope) = <u>-0.485</u> a (intercept) = <u>0.278 to 0.729</u>	M1 A1 A1		Correct attempt at 4 summations Correct attempt at 2 summations CAO AWFW
Notes	1 Values of a and b interchanged or not identified but equation $y = ax + b$ stated \Rightarrow max of 3 marks 2 Values of a and b interchanged or not identified and equation $y = a + bx$ stated \Rightarrow 0 marks 3 $y = 0.504 - 0.485$ or $0.504 - 0.485x$ stated without working \Rightarrow 2 marks 4 $x = 1.20 - 2.04y$ (OE) or $y = 1.20 - 2.04x$ (OE) \Rightarrow 0 marks		3	
(ii)	For each unit increase in (concentration of) antifreeze freezing point decreases by $ b ^\circ\text{C}$ or freezing point increases by $b^\circ\text{C}$	B1 Bdep1		OE OE; dep on $-0.47 \leq b \leq -0.50$
SC	1 As the percentage of antifreeze increases, the freezing point decreases \Rightarrow B1 (must be in context, not simply x and y)			
(c) (i)	$\text{Res}(15, -6.3) = -6.3 - (a + b \times 15)$ $=$ <u>+0.46 to +0.48</u> $=$ <u>(+0.02 to +0.93)</u> or <u>(-0.02 to -0.93)</u>	B2 (B1)	2	AWFW; do not ignore sign (0.47143) AWFW; either
(ii)	$\text{Sum}_5 = 0 - [-0.65 + (\text{c})(\text{i})]$ $=$ <u>+0.17 to +0.19</u> $=$ <u>-0.17 to -0.19</u> or <u>+1.11 to +1.13</u>	B2 (B1)	2	Or sum of remaining 5 residuals $(-0.504, -0.179, 0.246, 0.896, -0.279)$ AWFW; do not ignore sign (0.18214) AWFW; do not ignore sign
SC	1 Use of $\text{Sum}_7 = 0$ to obtain (realistic) $\text{Sum}_5 = -\text{Sum}_2 \Rightarrow$ M1			