

# A Level Statistics

## AQA Past Exam Questions

### Solutions

#### TOPIC: Least Squares Regression

In the new specification you will not be asked to calculate the values of  $a$  and  $b$  in any way other than on the calculator  
You will not be asked to plot or draw a scatter graph or the LSR on a scatter graph so these questions from past paper have been omitted

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have retrievable mathematical formulae stored in them.

#### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions **on paper**
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Unless otherwise stated, statistical tests should be carried out at the 5% significance level.
- When a calculator is used, the answer should be given to three significant figures unless otherwise stated.

#### Information

- **You may use the** booklet 'Statistical Formulae and Tables'
- There are **12** questions in this question paper. The total mark for this paper is **123**
- The marks for **each** question are shown in brackets – use this as a guide as to how much time to spend on each question.

#### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.
- Check your answers if you have time at the end.

Q	Solution	Marks	Total	Comments
<b>5</b>	See supplementary sheet for alternative solutions and additional guidelines to parts (b), (d) and (e)			
<b>(a)</b>	Calorific value depends upon moisture content Moisture (content) is set/are fixed values	B1	1	Must be in context; <b>not</b> “it”, etc Use of $x$ and $y \Rightarrow$ B0
<b>(b)</b>	$b$ (gradient) = $-0.076$ $b$ (gradient) = $-0.07$ to $-0.08$  $a$ (intercept) = $5.35$ to $5.36$ $a$ (intercept) = $5.1$ to $5.6$  Thus $y = (5.35 \text{ to } 5.36) - 0.076x$	B2 (B1)  B2 (B1)  BF1	   5	AWRT; including $-ve$ sign ( $-0.07582$ ) AWFW; including $-ve$ sign <i>Treat rounding of correct answers as ISW</i> AWFW ( $5.35385$ ) AWFW F on $a$ and $b$ even if rounded
<b>(c)</b>	$a$ : calorific value of wood with zero/no moisture or dry maximum calorific value  $b$ : each 1(%) rise in moisture content reduces calorific value by $0.076$ MWh/tonne  As $x$ increases $y$ decreases	B1  B2 (B1)	 3	OE; $a \leq 0 \Rightarrow$ B0  In context and with values; F on $b$ $b \geq 0 \Rightarrow$ B0  Negative relationship/correlation
<b>(d)</b>	$y_{27} = 3.28$ to $3.32$ $= 2.5$ to $3.5$	B2 (B1)	2	AWFW ( $3.30659$ ) AWFW; even if by interpolation from original data giving likely values of 3 or 3.04
<b>(e)</b>	$r(35, 2.5) = -0.21$ to $-0.19$ $= 0.1$ to $0.3$	B2 (B1)	2	AWFW; including $-ve$ sign ( $-0.20000$ ) AWFW; ignore sign
<b>(f)</b>	Good/reasonable/accurate/correct/etc  Accept more positive qualifying adjectives	B1	1	OE; ignore reasoning  Very good (B1)      Not good (B0)
<b>(g)(i)</b>	Extrapolation/outside (observed) range (of $x$ )	B1	1	OE
<b>(ii)</b>	$y_{80} = -0.5$ to $-1$  Negative value for calorific value is impossible or More energy needed than is generated	B1  Bdep1	 2	AWFW ( $-0.71209$ )  OE; dependent on B1 Must be in context; negative value impossible $\Rightarrow$ Bdep0

Q	Solution	Marks	Total	Comments
<b>1</b>				
<b>(a)</b>	$a = \underline{30}$	B1	<b>1</b>	CAO
<b>(b)(i)</b>	$b$ (gradient) = $\underline{-0.64}$ $b$ (gradient) = $\underline{-0.6 \text{ to } -0.7}$  $a$ (intercept) = $\underline{31}$ $a$ (intercept) = $\underline{30 \text{ to } 32}$	B2 (B1)  B2 (B1)	<b>4</b>	CAO (-0.64) AFWW <i>Treat rounding of correct answers as ISW</i> <i>Written form of equation is <b>not</b> required</i> CAO (31) AFWW
	Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ ( $\sum y^2$ ) <b>or</b> Attempt at $S_{xx}$ & $S_{xy}$ ( $S_{yy}$ ) Attempt at <b>correct</b> formula for $b$ (gradient) $b$ (gradient) = $\underline{-0.64}$ $a$ (intercept) = $\underline{31}$	(M1)  (m1) (A1 A1)		225 7125 135 & <b>2415</b> (2643) (all 4 attempted)  1500 & <b>-960</b> (618) (both attempted)  CAO both
	<b>(ii)</b> Candle <b>length reduces</b> <b>by 0.64 (cm) per hour</b> Candle <b>burns 0.64 (cm) each/per hour</b> Candle <b>reduces by -0.64 (cm) each/per hour</b>  (Length, $y$ , cm) <b>decreases</b> with (time, $x$ , hours) <b>or</b> As (time, $x$ , hours) <b>increases</b> then (length, $y$ , cm) <b>decreases</b>	B1 BF1 (BF2) (BF1)  (B1)		OE; must be in context OE; must be in context OE; must be in context OE; must be in context (double -ve) F on $-0.6 \leq b \leq -0.7$ from (i)  OE; context <b>not</b> required B0 for reference only to correlation
<b>(iii)</b>	When $x = 50$ , $y = (31 \text{ or } 30) - 0.64 \times 50$ $= \underline{-1 \text{ or } -2}$ <b>or</b> When $y = 0$ , $x = 31 \div 0.64 = \underline{48 \text{ to } 48.5}$ <b>or</b> $30 \div 0.64 = \underline{46.8 \text{ to } 47}$	B1	<b>2</b>	CAO; accept <b>correct</b> comparison of 32 with either 30 or 31  AFWW  AFWW
	Claim <b>not</b> justified <b>or</b> -1 is impossible <b>or</b> value < 50  Claim cannot be answered due to uneven burning <b>or</b> unlikely to burn completely	Bdep1  (B1)		OE; dependent on previous B1  Extrapolation required

3(a)	<p> <math>b</math> (gradient) = 7.05  <math>b</math> (gradient) = 7(.00) to 7.1(0) </p> <p> <math>a</math> (intercept) = 2500 to 2502  <math>a</math> (intercept) = 2490 to 2510 </p> <p> <b>or</b>            Attempt at  <math>\sum x \quad \sum x^2 \quad \sum y \quad \&amp; \quad \sum xy \quad (\sum y^2)</math>  <b>or</b>            Attempt at <math>S_{xy}</math> &amp; <math>S_{yy}</math> (<math>S_{xx}</math>) </p> <p>           Attempt at <b>correct</b> formula for <math>b</math>            (gradient)  <math>b</math> (gradient) = 7.05  <math>a</math> (intercept) = 2500 to 2502 </p> <p>           Accept <math>a</math> &amp; <math>b</math> interchanged only if            identified correctly by a <b>clearly shown</b>  <b>equation</b> (stated answers are not            sufficient) in (b) </p>	<p>B2 (B1)</p> <p>B2 (B1)</p> <p>(M1)</p> <p>(m1)</p> <p>(A1)</p> <p>(A1)</p>	<p>4</p> <p>4</p> <p>2</p> <p>2</p>	<p>           AWRT (7.05134)            AFWF            Treat rounding of correct stated answers            as ISW            AFWF (2501.091)            AFWF </p> <p>           1351 268047 27034 &amp; 5269065            (105653202)            (all 4 attempted) </p> <p>           7304 &amp; 51503 (1247894)            (both attempted) </p> <p>           AWRT            AFWF </p> <p>           If <math>a</math> and <math>b</math> are not identified anywhere            in solution, then:  <math>7.05 \Rightarrow B1</math>  <math>2500 \text{ to } 2502 \Rightarrow B1</math> </p> <p>           Used            May be implied by correct answer </p> <p>           AFWF (3911.36) </p> <p>           (unreliable) requires (10% or equivalent) </p> <p>           Any one; or equivalent </p>
(b)	<p> <math>y_{200} = a + b \times 200</math>   <math>= 3890 \text{ to } 3930</math> </p>	<p>M1</p> <p>A1</p>	<p>2</p>	<p>           Used            May be implied by correct answer </p> <p>           AFWF (3911.36) </p>
(c)	<p>           Large residuals / residual range            suggest estimate may be unreliable  <b>or</b>            Largest residuals only small in relation to  <math>y</math>-values (10%)            so estimate may be reliable (unreliable) </p> <p> <b>Special Case:</b>            If B0 B0dep then:            Involves interpolation            Does not involve extrapolation            Within observed range </p>	<p>B1 B1dep</p> <p>B1 B1dep</p> <p>(B1)</p>	<p>2</p>	<p>           (unreliable) requires (10% or equivalent) </p> <p>           Any one; or equivalent </p>



<b>1(a)</b>	$b$ (gradient) = $-1.01$ to $-1(.00)$ $(b$ (gradient) = $-1.05$ to $-0.95)$  $a$ (intercept) = $53(.0)$ to $53.2$ $(a$ (intercept) = $52(.0)$ to $54(.0))$	B2 (B1)  B2 (B1)	4	AFWW (–1.00337)  AFWW (53.06736)
<b>OR</b>	Attempt at $\sum x$ , $\sum x^2$ , $\sum y$ and $\sum xy$ <b>or</b> Attempt at $S_{xx}$ and $S_{xy}$ Attempt at <b>correct</b> formula for $b$ (gradient) $b$ (gradient) = $-1.01$ to $-1(.00)$ $a$ (intercept) = $53(.0)$ to $53.2$  Accept $a$ and $b$ interchanged only if then identified correctly in part (b), but B2 in (b) does <b>not</b> necessarily imply 4 marks in (a)	(M1)   (m1) (A1) (A1)		180, 3986, 297 and 5552.7  386 and –387.3  AFWW AFWW
<b>(b)</b>	When $x = 21$ ,  $y = 31.7$ to $32.2$ $(y = 29.9$ to $34.1)$  Evidence of use of 21 in c's equation  <i>Special Cases (if seen):</i>  $y = \frac{33.0+30.7}{2} = 31.8$ to $31.9$  $y = 31.85$ without working	B2 (B1)  (M1)   (B1)  (B1)	2	AFWW (32.0) AFWW      AFWW; or equivalent

<b>5(a)</b>	Time taken depends upon temperature	B1	1	OE; <b>not</b> x set values
<b>(b)</b>	$b$ (gradient) = $-0.0873$ to $-0.087$ $b$ (gradient) = $-0.09$ to $-0.08$	B2 (B1)		AWFW $(-0.087\dot{2}\dot{7})$ AWFW; $-8.73^{-02} \Rightarrow$ B0
	$a$ (intercept) = $5.94$ to $5.96$ $a$ (intercept) = $5.6$ to $6.1$	B2 (B1)		AWFW $(5.95\dot{0}\dot{9})$ AWFW
	Attempt at $\sum x$ , $\sum x^2$ , $\sum y$ and $\sum xy$ or Attempt at $S_{xx}$ and $S_{yy}$ Attempt at correct formula for $b$ $b = -0.0873$ to $-0.087$ $a = 5.94$ to $5.96$	(M1)  (m1) (A1) (A1)	4	396, 16016, 30.9 and 958.8  1760 and $-153.6$  AWFW AWFW
	Accept $a$ and $b$ interchanged only if then identified correctly later in question			
<b>(c)(i)</b>	Each $1^\circ\text{C}$ rise in temperature results in an (average) decrease of $0.087\text{ m}$ ( $5\text{ s}$ ) in time taken for pellets to dissolve	B1 B1	2	Quantified rise in $x$ (results in) Decrease in $y$ OE
<b>(ii)</b>	$a$ is $y$ -value at $x = 0$ at which water is solid/ice/frozen so pellets cannot dissolve	B1 B1	2	Indication that it is $y$ at $x = 0$ Mention of solid or ice or frozen
<b>(d)(i)</b>	When $x = 30$ $y = 3.3$ to $3.4$ $y = 2.9$ to $3.7$	B2 (B1)		AWFW $(3.33\dot{2}\dot{7})$ AWFW
	If B0, use of their equation with $x = 30$	(M1)	2	
<b>(ii)</b>	When $x = 75$ $y < 0$ or negative which is impossible	B1 $\uparrow\text{Dep}\uparrow$ B1	2	OE  OE; <b>not</b> extrapolation



4(a)	$b$ (gradient) = $-0.5485$ to $-0.5475$ $b$ (gradient) = $-0.55$ to $-0.54$ Omission of $-ve$ sign	B2 (B1) (B0)		AWFW AWFW	( $-0.54814$ )
	$a$ (intercept) = $49.7$ to $49.9$ $a$ (intercept) = $49$ to $50$	B2 (B1)		AWFW AWFW	( $49.7982$ )
	<b>or</b> Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ ( $\sum y^2$ )	(M1)		305 14975 281 & <b>6980</b> ( $10173$ ) (all 4 attempted)	
	<b>or</b> Attempt at $S_{xx}$ & $S_{xy}$ Attempt at <b>correct</b> formula for $b$ (gradient) $b$ (gradient) = $-0.5485$ to $-0.5475$ $a$ (intercept) = $49.7$ to $49.9$	(m1) (A1) (A1)	4	AWFW AWFW	
	Accept $a$ & $b$ interchanged only if identified correctly by a <b>clearly shown equation</b> (stated answers are not sufficient) in (b) or (c)			If $a$ and $b$ not identified anywhere in question, then: $-0.5485$ to $-0.5475 \Rightarrow B1$ $49.7$ to $49.9 \Rightarrow B1$	
(b)	C's value of intercept from (a) providing $> 47$ <b>or</b> Value 50 stated even if (a) incorrect or not attempted	B1F	1	Accept value rounded to nearest integer	(50)
(c)	13 weeks $\Rightarrow$ 91 days	B1		Stated or used Accept a descriptive answer that includes 91 and a value in range	
	$y = -1.1$ to $+ 1.1$	B1		AWFW	( $-0.08254$ )
	<b>or</b> $y = 0 \Rightarrow x = 89$ to $93$	(B1)		AWFW	( $90.84942$ )
	$\Rightarrow$ 13 weeks (approximately)	(B1)		Accept a descriptive answer that includes a value in range and 13 Stated	
	<b>Note:</b> B1 B1 or (B1) (B1) are available even if (a) not attempted				
	Thus claim appears <b>justified</b>			Or equivalent; ignore reasoning unless contradictory	
	<b>or</b> Thus tablet likely to have <b>dissolved</b>	B1 dep		Dependent upon 2 <sup>nd</sup> B1 in (c) or 2 <sup>nd</sup> (B1) in (c)	
	<b>or</b> Extrapolation required so cannot comment	(B1)		Not dependent	
	<b>Note:</b> If (B1) for extrapolation maximum mark is 2; other mark available is for 91		3		



3	<p>(a) <math>b</math> (gradient) = <b>191</b>  <math>b</math> (gradient) = <b>190 to 192</b></p> <p><math>a</math> (intercept) = <b>115</b>  <math>a</math> (intercept) = <b>93 to 137</b></p> <p><b>OR</b></p> <p>Attempt at <math>\sum x</math> <math>\sum x^2</math> <math>\sum y</math> &amp; <math>\sum xy</math> (<math>\sum y^2</math>)  <b>or</b>  Attempt at <math>S_{xx}</math> &amp; <math>S_{yy}</math> (<math>S_{xy}</math>)</p> <p>Attempt at <b>correct</b> formula for <math>b</math> (gradient)  <math>b</math> (gradient) = <b>191</b>  <math>a</math> (intercept) = <b>115</b></p> <p>Accept <math>a</math> &amp; <math>b</math> interchanged only if identified and used correctly in (ii)</p>	B2 (B1)  B2 (B1)  (M1)  (m1) (A1) (A1)	4	<p>CAO  AWFW  <i>Treat rounding of correct answers as ISW</i>  CAO  AWFW</p> <p>154 3452 30219 &amp; <b>677042</b>  (133170091) (all 4 attempted)</p> <p>12224 &amp; <b>64</b> (2714668)  (both attempted)</p> <p>CAO  CAO</p> <p>If <math>a</math> and <math>b</math> are not identified anywhere in question, then:  190 to 192 <math>\Rightarrow</math> B1  93 to 137 <math>\Rightarrow</math> B1</p>
(ii)	<p><math>y_{24} = 115 + 191 \times 24</math>  = <b>£4699 or £4700</b>  = <b>£4650 to £4750</b>  <b>SC:</b> <math>(4290 + 5057)/2 = 4673</math> to <math>4674 \Rightarrow</math> B1</p> <p>If B0 but <b>clear evidence</b> of correct use of c's equation with <math>x = 24</math></p>	B2 (B1)  (M1)	2	<p>Either; ignore units (£4699)  AWFW</p>
(iii)	<p>(Maximum) <b>temperature</b> (in February) is likely to be/will be lower/different</p> <p>Must imply a temperature comparison with July</p>	B1	1	<p>Or equivalent; must be <b>clear indication</b> that (max) <b>temperature</b> is less than/different  Extrapolation/not July/not summer/winter/etc <math>\Rightarrow</math> B0</p>
(iv)	<p>Rainfall amount/wind strength/sunshine hours/daylight hours/opening times/day of week/visitor numbers/public holidays/school holidays/local attractions/etc</p> <p>Allow if at least 1 variable correctly identified</p>	B1	1	<p>Or equivalent  Accept any sensible reason; do <b>not</b> penalise for dubious 'variable name' so, for example, accept 'rainfall'  Minimum/average temp/etc <math>\Rightarrow</math> B0  Quality or price of food/staff/etc <math>\Rightarrow</math> B0</p>

<b>3</b>	<b>No MR or MC in this question</b>			
<b>(a)</b>	$b$ (gradient/slope) = <u><b>0.85</b></u> $b$ (gradient/slope) = <u><b>0.8 to 0.9</b></u>  $a$ (intercept) = <u><b>94.6 to 94.8</b></u> $a$ (intercept) = <u><b>93 to 97</b></u>	B2 (B1)  B2 (B1)		AWRT (0.85055) AFWW  AFWW (94.69602) AFWW
	Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ <b>or</b> Attempt at $S_{xx}$ & $S_{xy}$ Attempt at <b>correct</b> formula for $b$ $b = \underline{\mathbf{0.85}}$ (AWRT) $a = \underline{\mathbf{94.6 to 94.8}}$ (AWFW)	(M1)  (m1)  (A1 A1)	<b>4</b>	254 6924 1163 & <b>29942</b> (all 4 attempted) ( $\sum y^2 = 135693$ )  472.4 & <b>401.8</b> (both attempted) ( $S_{yy} = 436.1$ )  ( $\bar{x} = 25.4$ & $\bar{y} = 116.3$ )
<b>Notes</b>	<b>1</b> Treat rounding of correct answers as ISW <b>2</b> Written form of equation is <b>not</b> required <b>3</b> Award 4 marks for $y = (94.6 \text{ to } 94.8) + 0.85$ or for $(94.6 \text{ to } 94.8) + 0.85x$ <b>4</b> Values of $a$ and $b$ interchanged and equation $y = ax + b$ stated in (b) $\Rightarrow$ max of 4 marks <b>5</b> Values of $a$ and $b$ interchanged and equation $y = a + bx$ stated in (b) $\Rightarrow$ 0 marks <b>6</b> Values are <b>not</b> identified or simply $b/a = \#$ and $a/b = \#$ , then 0.8 to 0.9 $\Rightarrow$ B1 and 93 to 97 $\Rightarrow$ B1 but accept, for example, as identification, $[b = \#, a = \# \text{ with } y = a + bx \text{ but no substitution for } b \text{ \& } a]$ <b>or</b> $[\text{slope/gradient}(b) = \#, \text{intercept}(a) = \#]$ <b>7</b> Answers in fractions can score at most M1 m1 <b>8</b> Some/all of marks can be scored in (b) & (d), even if some/all of marks are lost in (a), but marks lost in (a) <b>cannot</b> be recouped by subsequent working in (b) or (d)			
<b>(b)</b>	$y_{30} = \underline{\mathbf{120 to 120.5}}$ $y_{30} = \underline{\mathbf{117 to 123}}$	B2 (B1)	<b>2</b>	AFWW (120.21253) AFWW
<b>Note</b>	<b>1</b> If, and only if, B0, then award M1 for seen use of $y = a + b \times 30$			
<b>(c)(i)</b>	<b>Extrapolation</b> <b>BMI is outside/above range</b> <b>45 is outside/above range of BMI or x</b>	B1		OE; accept references to sample/data but not to population
<b>(ii)</b>	<b>Extrapolation</b> <b>Age is outside/above range</b> <b>50 is outside/above range of age</b>	B1		OE; accept references to sample/data but not to population
<b>Notes</b>	<b>1</b> Extrapolation only stated in each of (i) & (ii) $\Rightarrow$ B1 B0 <b>2</b> Two debateable answers $\Rightarrow$ B1 max			
<b>(d)</b>	$r_{20} = 117 - (a + b \times 20) = \underline{\mathbf{5.3}}$ $= \underline{\mathbf{5 to 6}}$	B2 (B1)	<b>2</b>	AWRT; do not ignore sign (5.29297) AFWW; ignore sign
<b>Note</b>	<b>1</b> If, and only if, B0, then award M1 for seen use of $\pm[117 - (a + b \times 20)]$			
<b>(e)</b>	As 2.71/(mean) value is small (in comparison to y-values), estimate is likely to be (quite/fairly/very/extremely) accurate	B1	<b>1</b>	OE; justification & conclusion

5(a) (i)	$b$ (gradient/slope) = <u>0.372 to 0.373</u> $b$ (gradient/slope) = <u>0.3 to 0.4</u>  $a$ (intercept) = <u>6.94 to 6.95</u> $a$ (intercept) = <u>6 to 9</u>	B2 (B1)  B2 (B1)		AFWW (0.37235) AFWW  AFWW (6.94648) AFWW
	Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ or Attempt at $S_{xx}$ & $S_{yy}$  Attempt at substitution into correct corresponding formula for $b$ $b = \underline{0.372 \text{ to } 0.373}$ $a = \underline{6.94 \text{ to } 6.95}$	(M1)  (m1) (A1 A1)	4	324 8922.70 204 & <b>5573.05</b> (all 4 attempted) ( $\sum y^2 = 3493.64$ ) 174.70 & <b>65.05</b> (both attempted) ( $S_{yy} = 25.64$ )  AFWW ( $\bar{x} = 27$ & $\bar{y} = 17$ )
Notes	1 Written form of equation is <b>not</b> required 2 Award 4 marks for $y = (6.94 \text{ to } 6.95) + (0.372 \text{ to } 0.373)x$ or for $(6.94 \text{ to } 6.95) + (0.372 \text{ to } 0.373)x$ 3 Values of $a$ and $b$ interchanged and equation $y = ax + b$ <b>stated or used in (b) or (c)</b> $\Rightarrow$ max of 4 marks 4 Values of $a$ and $b$ interchanged and equation $y = a + bx$ <b>stated or used in (b) &amp; (c)</b> $\Rightarrow$ 0 marks 5 Values are <b>not</b> identified, then $\Rightarrow$ B0 B0 6 Some/all of marks can be scored in (a)(ii), (a)(iii), (b) & (c)(i), even if some/all of marks are lost in (a)(i), but marks lost in (a)(i) <b>cannot</b> be recouped by subsequent working in (a)(ii), (a)(iii), (b) or (c)(i) but see <b>Note 3</b>			
(ii)	<b>Each/every/one degree (<math>^{\circ}\text{C}</math>) rise</b> <b>in ground temperature results in</b> <b>or increase per degree (<math>^{\circ}\text{C}</math>) is</b> <b>(on average) <math>b</math> vibrations per second</b>	B1  BF1	2	F on $b$ providing $0.3 \leq b \leq 0.4$
Notes	1 To score any marks, an explanation must indicate change in $x$ affecting change in $y$ , <b>not</b> change in $y$ affecting change in $x$ 2 Accept, for example, $10^{\circ}\text{C}$ and 10 <i>b</i> vibrations 3 Reference <b>only</b> to correlation $\Rightarrow$ B0 BF0			
SC	1 As $x$ /temperature increases (by $c$ ) then $y$ /vibrations increases by $b$ (OE; value of $b$ ( $0.3 \leq b \leq 0.4$ ) must be stated but context and/or units are <b>not</b> required) $\Rightarrow$ B1			
(iii)	<u>Given:</u> When temperature/ $x < 15^{\circ}\text{C}$ or $= 0^{\circ}\text{C}$ value of <u><math>y = 0</math></u>  <u>Equation:</u> When temperature/ $x = 0^{\circ}\text{C}$ vibrations/value of <u><math>y = 6 \text{ to } 9</math></u>	B1  BF1	2	<b>Must be stated clearly</b>  AFWW F on $a$ providing $6 \leq a \leq 9$
Notes	1 B1 is for a <b>clear statement</b> of information given in the question in terms of temperature/ $x$ and $y$ 2 BF1 is for a <b>clear statement</b> of the value of vibrations/ $y$ shown by the equation when temperature/ $x = 0$			
5	<b>Continued</b>			
	<b>Part (a)</b>	<b>Total</b>	<b>8</b>	
(b)	$y(23) = \underline{15.4 \text{ to } 15.6}$	B1	1	AFWW (15.51059)
Note	1 Ignore any method shown			
(c) (i)	$\text{res}(28.6) = 17.0 - a - b \times 28.6$ $= \underline{-0.55 \text{ to } -0.65}$ $= \underline{0.5 \text{ to } 0.7}$	B2 (B1)	2	AFWW; do <b>not</b> ignore sign ( $-0.59576$ ) AFWW; ignore sign
Note	1 If, and only if, B0, then attempted use of $\pm(17.0 - a - b \times 28.6) \Rightarrow$ M1 providing $0.3 \leq b \leq 0.4$ and $6 \leq a \leq 9$			
(ii)	Value will be/is always:  <u>0 or zero or nought or nothing or nil</u>	B1	1	CAO; accept nothing else, but ignore zeros after decimal point (eg 0.00) Ignore any explanation

2 (a)	$b$ (gradient/slope) = <u><math>-0.574</math> to <math>-0.575</math></u> $b$ (gradient/slope) = <u><math>-0.5</math> to <math>-0.6</math></u>  $a$ (intercept) = <u><math>50.9</math> to <math>51.0</math></u> $a$ (intercept) = <u><math>46</math> to <math>53</math></u>  <u><math>y = (46 \text{ to } 53) - (0.5 \text{ to } 0.6)x</math></u>  OR	B2 (B1)  B2 (B1)  B1		AWFW AWFW  AWFW AWFW   
	Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ or Attempt at $S_{xx}$ & $S_{xy}$ Attempt at substitution into correct corresponding formula for $b$ $b = \underline{-0.574 \text{ to } -0.575}$ $a = \underline{50.9 \text{ to } 51.0}$  <u><math>y = (46 \text{ to } 53) - (0.5 \text{ to } 0.6)x</math></u>	(M1)  (m1)  (A1 A1)  B1	5	570 32825.1 182 & <b>10181.48</b> (all 4 attempted)      ( $\sum y^2 = 3441.64$ ) 335.1 & <b>-192.52</b> (both attempted)      ( $S_{yy} = 129.24$ )  AWFW      ( $\bar{x} = 57$ & $\bar{y} = 18.2$ )
<b>Notes</b>	<b>1</b> Values of $a$ and $b$ interchanged or not identified but equation $y = ax + b$ <b>stated</b> $\Rightarrow$ max of 5 marks <b>2</b> Values of $a$ and $b$ interchanged or not identified and equation $y = a + bx$ <b>stated</b> $\Rightarrow$ 0 marks			
(b) (i)	$y_{(60.0)} = \underline{16.3 \text{ to } 16.6}$	B1	1	AWFW (16.476455)
(ii)	<u>Women/sample selected could be:</u>  Under 45    or    Over 65 or Not between 45 and 65  No previous browsing/IT experience or No internet/IT access	B1   B1	2	   OE; must reference age/years   Accept "less experience" OE Accept "limited access"

5				
(a)	$x$ is the <b>independent/controlled</b> variable $x$ are <b>set values/percentages</b> $y$ is the <b>response/dependent</b> variable $y$ are <b>measured values/degrees</b> $y$ <b>depends on <math>x</math> or <math>x</math> does not depend on <math>y</math></b>	B1	1	OE
(b)				
(i)	$b$ (gradient/slope) = <u><math>-0.485</math></u> $b$ (gradient/slope) = <u><math>-0.47</math> to <math>-0.50</math></u>  $a$ (intercept) = <u><math>0.278</math> to <math>0.729</math></u>  <b>or</b> $\sum x = 105$ $\sum x^2 = 2275$ ( $\sum y^2 = 487.5$ ) $\sum y = -47.4$ $\sum xy = -1050.5$ <b>or</b> $S_{xx} = 700$ $S_{yy} = -339.5$ ( $S_{yy} = 166.53429$ ) $b$ (gradient/slope) = <u><math>-0.485</math></u> $a$ (intercept) = <u><math>0.278</math> to <math>0.729</math></u>	B2 (B1)  B1    M1    A1 A1	3	CAO AFWW  AFWW (0.50357)   Correct attempt at 4 summations  Correct attempt at 2 summations  CAO AFWW
Notes	1 Values of $a$ and $b$ interchanged or not identified but equation $y = ax + b$ <b>stated</b> $\Rightarrow$ max of 3 marks 2 Values of $a$ and $b$ interchanged or not identified and equation $y = a + bx$ <b>stated</b> $\Rightarrow$ 0 marks 3 $y = 0.504 - 0.485$ or $0.504 - 0.485x$ stated without working $\Rightarrow$ 2 marks 4 $x = 1.20 - 2.04y$ (OE) or $y = 1.20 - 2.04x$ (OE) $\Rightarrow$ 0 marks			
(ii)	For each <b>unit increase</b> in (concentration of) <b>antifreeze</b>  <b>freezing point decreases by <math> b ^\circ\text{C}</math></b> <b>or</b> <b>freezing point increases by <math>b^\circ\text{C}</math></b>	B1  Bdepl	2	OE  OE; dep on $-0.47 \leq b \leq -0.50$
SC	1 As the percentage of antifreeze increases, the freezing point decreases $\Rightarrow$ B1 (must be in context, not simply $x$ and $y$ )			
(c)				
(i)	$\text{Res}(15, -6.3) = -6.3 - (a + b \times 15)$ $=$ <u><math>+0.46</math> to <math>+0.48</math></u>  $=$ <u><math>(+0.02</math> to <math>+0.93)</math> or <math>(-0.02</math> to <math>-0.93)</math></u>	B2  (B1)	2	AFWW; do not ignore sign (0.47143)  AFWW; either
(ii)	$\text{Sum}_5 = 0 - [-0.65 + (c)(i)]$  $=$ <u><math>+0.17</math> to <math>+0.19</math></u>  $=$ <u><math>-0.17</math> to <math>-0.19</math> or <math>+1.11</math> to <math>+1.13</math></u>	B2  (B1)	2	Or <b>sum</b> of remaining 5 residuals ( $-0.504, -0.179, 0.246, 0.896, -0.279$ )  AFWW; do not ignore sign (0.18214)  AFWW; do not ignore sign
SC	1 Use of $\text{Sum}_7 = 0$ to obtain (realistic) $\text{Sum}_5 = -\text{Sum}_2 \Rightarrow$ M1			